Enhanced Regional Ocean Ensemble Data Assimilation Through Atmospheric Coupling in the SKRIPS Model

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10 Abstract

We investigate the impact of ocean data assimilation using the Ensemble Adjustment 11 Kalman Filter (EAKF) from the Data Assimilation Research Testbed (DART) on the 12 oceanic and atmospheric states of the Red Sea. Our study extends the ocean data as-13 similation experiment performed by Sanikommu et al. (2020) by utilizing the SKRIPS 14 model coupling the MITgcm ocean model and the Weather Research and Forecasting (WRF) 15 atmosphere model. Using a 50-member ensemble, we assimilate satellite-derived sea sur-16 face temperature and height and in-situ temperature and salinity profiles every three days 17 for one year, starting January 01 2011. Atmospheric data are not assimilated in the ex-18 periments. To improve the ensemble realism, perturbations are added to the WRF model 19 using several physics options and the stochastic kinetic energy backscatter (SKEB) scheme. 20 Compared with the control experiments using uncoupled MITgcm with ECMWF ensem-21 ble forcing, the EAKF ensemble mean oceanic states from the coupled model are bet-22 ter or insignificantly worse (root-mean-square errors are 30% to -2% smaller), especially 23 when the atmospheric model uncertainties are accounted for with stochastic perturba-24 tions. We hypothesize that the ensemble spreads of the air-sea fluxes are better repre-25 sented in the downscaled WRF ensembles when uncertainties are well accounted for, lead-26 ing to improved representation of the ensemble oceanic states from the new experiments 27 with the coupled model. This indicates the ocean model assimilation will be improved 28 with coupled models and relaxes the need for operational centers to provide atmospheric 29 ensembles to drive ocean forecasts. Although the feedback from ocean to atmosphere is 30 included in this two-way regional coupled configuration, we find no significant effect of 31 ocean data assimilation on the ensemble mean latent heat flux and 10-m wind speed over 32 the Red Sea. This suggests that the improved skill using the coupled model is not from 33 the two-way coupling, but from downscaling the ensemble atmospheric forcings (one-way 34 coupled) to drive the ocean model. 35

³⁶ Plain Language Summary

We investigate how combining ocean information accounting for weather processes 37 can help us better understand and predict the ocean-atmospheric state of the Red Sea. 38 We use a coupled ocean and atmosphere model to assimilate satellite and ship-based ocean 39 observations. We assess the performance of the assimilation system using fifty different 40 realizations of the atmospheric state and found that it improves the prediction of oceanic 41 state compared to using the ocean model alone for assimilation and prediction. This suc-42 cess is because the combined ocean-atmosphere model provides a broader range of pos-43 sible ocean conditions. We also look at how incorporating ocean observation informa-44 tion may potentially impact weather forecasts in the coupled model. 45

46 1 Introduction

Numerical models have been used to analyze and predict ocean states for decades. 47 Realistically configured numerical models can simulate oceanic conditions that are gen-48 erally consistent with observations, but there can be substantial differences when com-49 paring with observations at specific times and locations (Edwards et al., 2015). Even with 50 a perfect model, the differences can result from uncertainties of initial conditions, per-51 turbations, parameterizations, and forcings. Because of this, data assimilation (DA) is 52 used to constrain the model solutions using observational data, including observation un-53 certainty and model representational error (Edwards et al., 2015). 54

The Ensemble Kalman Filter (hereafter EnKF) provides an efficient framework for ocean data assimilation (Evensen, 1994). It has gained popularity because of its simple conceptual formulation and relative ease of implementation, requiring no derivation of tangent linear or adjoint models, with only forward model integration in time (Evensen, 2003). Furthermore, its computational requirements scale with ensemble size, and so can

be affordable and comparable with other popular sophisticated assimilation methods (Evensen, 60 2003). EnKF based data assimilation systems have been developed for many applica-61 tions. For example, Evensen and Van Leeuwen (1996) assimilated altimeter data in the 62 Agulhas region using a quasi-geostrophic model; Sakov et al. (2012) and Hoteit et al. (2013) 63 respectively produced realistic estimates of the ocean circulation in the North Atlantic 64 and the Gulf of Mexico; Sanikommu et al. (2020) investigated the impact of atmospheric 65 forcing and model physics perturbations using an Ensemble Adjustment Kalman Filter (EAKF). 66 In addition to ocean data assimilation, EnKF is used for operational atmospheric assim-67 ilation at the Canadian Meteorological Centre (Houtekamer et al., 2005) among many 68 other applications (e.g., Lawson & Hansen, 2004; Leeuwenburgh et al., 2005; Bannister, 69 2017). 70

A major component of EnKF data assimilation systems is the background error 71 covariance estimated from the ensembles (Bannister, 2008a, 2008b; Song et al., 2010). 72 EnKFs can suffer from the collapse of the ensemble spread, which unrealistically reduces 73 the background error covariance in the data assimilation system (e.g., J. Anderson & An-74 derson, 1999; Hoteit et al., 2002). This is often mitigated using covariance inflation tech-75 niques to increase the ensemble spread to better describe the background covariance (J. An-76 derson & Anderson, 1999; Hoteit et al., 2002; F. Zhang et al., 2004; Whitaker & Hamill, 77 2012; Luo & Hoteit, 2012). A more representative approach is to account directly for un-78 certainties in the model, such as the forcing and boundary conditions. Diverse high-resolution 79 forcings that represent the uncertainty of the atmosphere are indeed desirable for ocean 80 ensemble data assimilation system. Many studies have demonstrated improved forecasts 81 and analyses when driving ensemble ocean data assimilation systems with perturbed at-82 mospheric forcing (Lisæter et al., 2003; Evensen, 2004; Wan et al., 2008; Shu et al., 2011; 83 Sakov et al., 2012; Karspeck et al., 2013; Penny et al., 2015; Sanikommu et al., 2017, 2019). 84 Others investigated the perturbed model physics (Sandery et al., 2014; Brankart et al., 85 2015; Lima et al., 2019), or combined the perturbations of atmospheric forcing and model 86 physics (Vandenbulcke & Barth, 2015; K. M. Kwon et al., 2016; Sanikommu et al., 2020). 87 A recent study by Sanikommu et al. (2020) performed a detailed analysis of the impacts 88 of model physics perturbations and atmospheric forcing on a high-resolution regional ocean 89 DA system. The DA experiments improved the forecasts of oceanic states by using mul-90 tiple oceanic model physics and ensemble atmospheric forcing now available from oper-91 ational weather systems. 92

Our study takes a step forward toward a fully coupled ocean-atmospheric data as-93 similation system, with application to the Red Sea region. A regional assimilation sys-94 tem is crucial for improving forecasts in the Red Sea due to its unique characteristics in 95 terms of both oceanic and atmospheric conditions (Hoteit et al., 2021). The region is prone 96 to dust and sandstorms, particularly during the transitional seasons of spring and au-97 tumn, originating from nearby deserts like the Sahara. These storms significantly reduce 98 visibility and impact air quality (Prakash et al., 2014). The Red Sea also experiences fre-99 quent temperature inversions, especially in winter, which affect temperature profiles, pol-100 lutant dispersal, and vertical mixing of air masses. The region is influenced by two pri-101 mary wind patterns: the Southwest Monsoon, bringing humid air and thunderstorms, 102 and the Northwest Monsoon, bringing drier air (Langodan et al., 2017). A sea breeze 103 often develops during the day, cooling coastal areas (Davis et al., 2019). The Red Sea 104 warm surface waters contribute to high levels of water vapor, impacting local weather 105 conditions and precipitation. The local atmospheric features vary significantly with sea-106 sons, weather patterns, and local geography (Dasari et al., n.d.). The Red Sea holds eco-107 nomic importance and plays a vital role in international trade. Further, the Red Sea cir-108 culation plays a dominant role in modifying the salinity budgets of the western Indian 109 Ocean. Global reanalysis often fails to capture the Red Sea circulation features accurately 110 due to coarse resolutions and limited observations (Sanikommu et al., 2023a). Develop-111 ing a high-resolution regional reanalysis using local observations and coupled ocean-atmospheric 112

data assimilation system would greatly enhance the forecasts in the Red Sea, and this is important for many applications in this unique region.

In this context, we implement a new ensemble DA system for the Red Sea using 115 the Scripps-KAUST Regional Integrated Prediction System (SKRIPS, Sun et al., 2019, 116 2023) and the Data Assimilation Research Testbed (DART, J. Anderson et al., 2009). 117 This work is an extension of previous DA efforts for the Red Sea (Toye et al., 2017; Sanikommu 118 et al., 2020, 2023b), replacing the uncoupled ocean model with the SKRIPS coupled model (Sun 119 et al., 2019, 2023). Here we assimilate only oceanic observations using the DART–EAKF 120 121 system and investigate the estimated oceanic and atmospheric states of the Red Sea regional coupled model, using different options to perturb the physics of the atmosphere 122 model. We evaluate the performance of the coupled model in forecasting the oceanic states, 123 the impact of atmospheric model physics options on the coupled model, and the feed-124 back of the ocean data assimilation to the atmospheric model. Although we only assim-125 ilate ocean observations in this work, the present study is a step toward developing a weakly 126 coupled DA system and operational analysis and forecasting system for the Red Sea. Be-127 cause the random atmospheric states are generated by perturbing the model physics when 128 using a coupled model, there is less need to generate large ensembles of atmospheric forc-129 ings (Sanikommu et al., 2023a), enhancing the robustness of the DA system. 130

The rest of the manuscript is organized as follows. We first introduce the ensemble DA system and its implementation in Section 2. The results of the DA experiments are presented and discussed in Section 3. The final section outlines the main findings and concludes this work.

¹³⁵ 2 Implementations and Experimental Design

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2.1 The Data Assimilation Framework

We use the SKRIPS model (Sun et al., 2019) for the coupled simulation: the oceanic 137 model component is the MIT general circulation model (MITgcm, Marshall et al., 1997; 138 Campin et al., 2019) and the atmospheric model component is the Weather Research and 139 Forecasting (WRF) model (Skamarock et al., 2019). The Earth System Modeling Frame-140 work (ESMF, Hill et al., 2004) and the National United Operational Prediction Capa-141 bility (NUOPC) layer are used to handle the coupling between MITgcm and WRF. The 142 schematic diagram of the DART-SKRIPS framework and the domain used in the exper-143 iment are shown in Fig. 1. The ocean data are assimilated using EAKF available from 144 the DART-MITgcm package (Hoteit et al., 2013, 2015), aiming to evaluate their impact 145 on the ocean and atmosphere states in the coupled system. The ROCOTO workflow (Harrop 146 et al., 2017) is used for the management of the pre- and post-processing scripts in the 147 developed DART–SKRIPS framework. 148

The coupled model is also described in the diagram shown in Fig. 1. In the cou-149 pling process, MITgcm sends sea surface temperature (SST) and ocean surface veloc-150 ity to WRF; WRF sends air-sea flux and surface atmospheric fields to MITgcm, includ-151 ing (1) net surface longwave and shortwave radiative fluxes, (2) surface latent and sen-152 sible heat fluxes, (3) 10-m wind speed, (4) precipitation, and (5) evaporation. The MIT-153 gcm model uses the surface atmospheric variables to prescribe surface forcing, includ-154 ing (1) total net surface heat flux, (2) surface wind stress, and (3) freshwater flux. The 155 total net surface heat flux is computed by adding surface latent heat flux, sensible heat 156 flux, net shortwave radiation flux, and net longwave radiation flux. The surface latent 157 and sensible heat fluxes are computed using the COARE 3.0 bulk algorithm in WRF (Fairall 158 et al., 2003). 159



Figure 1. The schematic description of the DART–SKRIPS data assimilation system. Panel (a) indicates the DART–SKRIPS framework: the blue blocks denote the SKRIPS model, DART, and ocean observations; the yellow block is the ESMF/NUOPC coupler; the white blocks are the ocean and atmosphere components; the red blocks are the implemented MITgcm–ESMF and WRF–ESMF interfaces. The arrows indicate the information exchange between DART and SKRIPS. Panel (b) shows the workflow at three time steps: the thick solid line indicates the evolution of the "truth"; the dashed line indicates the ensemble averaged forecast; the thin solid lines indicate the evolution of the ensemble members; the red dots indicate the analysis; the shaded areas indicate the error covariance; t_k , t_{k+1} , and t_{k+2} indicate three steps when observational data are assimilated. Panel (c) shows the domain of the coupled model, with the black line indicating the centerline of the Red Sea.

2.2 Experimental Design

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To study the impact of ocean data assimilation on the oceanic and atmospheric states. 161 we perform a series of 50-member ensemble DA experiments using coupled and uncou-162 pled models starting from January 01 2011, assimilating the observational data every 3 163 days. For the coupled model experiments, the ocean and atmosphere models are nested 164 in GLORYS and ERA5 reanalyses, respectively. For the uncoupled model experiments, 165 the ocean model is also nested in GLORYS, but driven by ECMWF derived atmospheric 166 forcing. Further details on the initial and boundary conditions will be discussed in the 167 latter sections. The same setup is used for the ocean model, but different options are used 168 for the atmosphere in the 50-member ensemble DA experiments: 169

- 170 1. OCN.daO uses only the ocean model forced by the ECMWF ensemble mean.
 - 2. OCN.daF uses only the ocean model forced by the 50-member ECMWF ensembles.
 - 3. CPL.daO uses the coupled model with no perturbations to the atmosphere.
 - 4. CPL.daS uses the coupled model with stochastic forcings in the atmospheric model.
 - 5. CPL.daP uses the coupled model with perturbed physics options in the atmospheric
 - model (e.g., microphysics, convection, and planetary boundary layer).
- 6. CPL.daSP uses the coupled model with stochastic forcings and perturbed atmo sphere physics options.

OCN.daO and OCN.daF follow the experiments using the ocean-only models in Sanikommu 179 et al. (2020), but without inflation to investigate the changes using the coupled model. 180 They also serve as benchmarks to evaluate the performance of the coupled experiments. 181 In the coupled DA experiment CPL.daO, although we did not perturb the atmospheric 182 model physics, the randomness of the atmospheric forcing is from the feedback of dif-183 ferent ocean states. Different random seeds are used for the stochastic model in CPL.daS 184 and CPL.daSP from 1 to 50. The coupled DA experiments OCN.daS, OCN.daP, and OCN.daSP 185 are conducted to assess the effect of different strategies of the atmospheric forcings, and 186 thus we did not assimilate the atmospheric observational data in our experiments. Al-187 though the ocean feedback is important in the coupled model, we did not perform DA 188 experiments driven by the atmospheric forcings from stand-alone WRF models because 189 it is out of the scope of our work. 190

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2.3 The Forward Models

The initial conditions, boundary conditions, and forcings are outlined in Table 1. 192 The MITgcm initial conditions are obtained from a spin-up run as described in Sanikommu 193 et al. (2020), with randomly selecting 50 ocean states corresponding to ± 15 days from 194 the initial time. The boundary conditions for the ocean are updated by linearly inter-195 polating between the daily data from Global Ocean Reanalysis and Simulation (GLORYS, 196 Jean-Michel et al., 2021). For the uncoupled experiments, the atmospheric forcings are 197 from the ECMWF atmospheric ensemble from The Observing System Research and Pre-198 dictability Experiment Interactive Grand Global Ensemble project (TIGGE, Bougeault 199 et al., 2010), with full details available in Buizza (2014). We combined the fields of the 200 00 and 12 UTC TIGGE initial conditions and 06 and 18 UTC forecasts as 6-hourly forc-201 ing for our ocean ensemble assimilation runs. For OCN.daO, we forced the model with 202 the ensemble mean of the atmospheric forcings; for OCN.daF, we forced the model with 203 the ECMWF 50-member ensembles. In the coupled experiments, ERA5 provides the ini-204 tial and boundary conditions for the atmosphere model, with the atmospheric bound-205 ary conditions updated by linearly interpolating between the 6-hourly fields. Spectral 206 nudging is not used in the DA experiments because (1) nudging may constrain the high 207 frequency internal variability of the atmosphere model and (2) the domain size is com-208 parable with wavelengths typically used in the spectral nudging simulations (Liu et al., 209 2012).210

We choose the latitude-longitude (cylindrical equidistant) map projection to gen-211 erate the grids for MITgcm and WRF. The domains for both models extend from 10° N 212 to 30° N and from 30° E to 50° E. In the ocean model, the horizontal grid has 500×500 213 $(lat \times long)$ cells and the spacing is about 4 km; in the atmospheric model, the horizon-214 tal grid has 125×125 (lat \times long) cells and the spacing is about 16 km. There are 40 sigma 215 layers in the atmospheric model (top pressure is 50 hPa) and 50 z-layers in the ocean 216 model (dz = 4 m at the top). The time step of the oceanic model is 200 seconds; the 217 time step of the atmospheric model is 25 seconds; the coupling interval is 200 seconds. 218

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2.4 Model Perturbations

For the oceanic simulations in all DA experiments, we use various physical param-220 eterization schemes to account for the effects of unresolved scales of motion as proposed 221 by Sanikommu et al. (2020), summarized in Table 2. Three different categories of model 222 physics are selected: horizontal viscosity, vertical mixing, and horizontal diffusion. We 223 include three different horizontal viscosity schemes: the simple harmonic scheme, the sim-224 225 ple biharmonic of Holland (1978), and the Smagorinsky/Leith scheme (Smagorinsky et al., 1993; Griffies & Hallberg, 2000) with the coefficients suggested in the literature (Leith, 226 1996; Griffies & Hallberg, 2000). For vertical mixing, four different schemes are included: 227 the nonlocal K-Profile Parameterization (KPP) scheme (W. G. Large et al., 1994), the 228 PP81 scheme (Pacanowski & Philander, 1981), the MY82 scheme (Mellor & Yamada, 229

1982), and the GGL90 scheme (Gaspar et al., 1990). For the horizontal diffusion, we use
implicit diffusion, simple-explicit harmonic diffusion, and three different flavors of GentMcWilliams/Redi subgrid-scale eddy parameterization schemes (hereafter GMREDI, Gent & McWilliams, 1990; Gent et al., 1995; Redi, 1982): the GMREDI clipping scheme of Cox
(1987), the GMREDI-dm95 tapering scheme of Danabasoglu and McWilliams (1995),
and the GMREDI-ldd92 tapering scheme of W. Large et al. (1997). Table 2 lists the coefficients used in these schemes.

We also perturb the physics options in WRF to parameterize microphysics, con-237 vection, and planetary boundary layer (PBL), summarized in Table 3. For the micro-238 physics we use the Morrison 2-moment scheme (Morrison et al., 2009), the Purdue-Lin 239 scheme (Chen & Sun, 2002), the Thompson scheme (Thompson et al., 2008), the WRF 240 single moment 6-class scheme (Hong & Lim, 2006), and the WRF double moment 6-class 241 scheme (Lim & Hong, 2010). For the cumulus convection, we use the Kain–Fritsch scheme (Kain, 242 2004), the Betts-Miller-Janjic scheme (Janjić, 1994), the Grell-Freitas Ensemble scheme (Grell 243 & Freitas, 2014), the new Tiedtke scheme (C. Zhang & Wang, 2017), and the simplified 244 Arakawa–Schubert scheme (Y. C. Kwon & Hong, 2017). For the planetary boundary layer, 245 we use the Mellor–Yamada Nakanishi Niino scheme (MYNN, Nakanishi & Niino, 2004, 246 2009), the Yonsei University scheme (Hong et al., 2006), and the Mellor–Yamada–Janjic 247 scheme (Janjić, 1994). The radiation and land surface schemes are not perturbed: the 248 Rapid Radiation Transfer Model for GCMs (RRTMG, Iacono et al., 2008) is used for long-249 wave and shortwave radiation transfer through the atmosphere; the Noah land surface 250 model is used for the land surface processes (Tewari et al., 2004). The physics scheme 251 perturbation is based on the ensemble forecast system of the Center For Western Weather 252 and Water Extremes (CW3E, Oakley et al., 2023). For the experiments without perturb-253 ing the atmospheric model (i.e., CPL.daO and CPL.daS), we use Morrison 2-moment 254 scheme, Kain–Fritsch scheme, and MYNN scheme for microphysics, convection, and PBL, 255 respectively. 256

In addition to perturbing the atmospheric model physics, we used the SKEB scheme (Shutts, 2005; Berner et al., 2009) to account for the unrepresented uncertainties in the model. This scheme adds stochastic, small-amplitude perturbations to the horizontal wind and potential temperature. The default amplitudes of the stochastic perturbations in WRF were used in CPL.daS and CPL.daSP, which were able to provide more reliable ensemble spreads (Berner et al., 2011, 2015).

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2.5 Data Used in Assimilation and Validation

We assimilate data from level-4 SST blended daily product available on a $0.25^{\circ} \times$ 264 0.25° grid (Reynolds et al., 2007; Banzon et al., 2016), along-track satellite altimeter level-265 3 sea level anomalies (SLAs; corrected for dynamic atmospheric loading, ocean tide, and 266 long wavelength errors) available from Copernicus Marine Environment Monitoring Ser-267 vice (here after CMEMS-L3, Mertz et al., 2017), and quality controlled in situ glider tem-268 perature and salinity profiles from EN4 data (Ingleby & Huddleston, 2007; Good et al., 269 2013). The in situ temperature and salinity profiles are sparse, and there are only 244 270 temperature and 110 salinity profiles in the entire year 2011 from the glider in the Red 271 Sea. Errors associated with these observations are assumed uncorrelated, so the obser-272 vational error covariance matrix is diagonal. The combined observation and represen-273 tation error variance is determined based on previous DA experiments (Toye et al., 2017; 274 Sanikommu et al., 2020) and accounts for errors due to: measurement devices, omitted 275 processes, unresolved subgrid scale dynamics, and numerical errors in interpolation. Tem-276 porally static, partially homogeneous, and depth independent observational error vari-277 ance values of $(0.5^{\circ}C)^2$, $(0.04 \text{ m})^2$, $(0.5^{\circ}C)^2$, and $(0.3 \text{ psu})^2$ are then used for satellite 278 SST, satellite along-track SLA, in situ temperature and salinity, respectively. A cutoff 279 radius of about 300 km was imposed to localize the impact the observations in the hor-280 izontal directly (not in the vertical) as a way to mitigate spurious correlations. 281

	OCN Experiments	CPL Experiments	
Model region	10° N to 30° N; 30° E to 50° E		
Grid size	500×500	500×500 for ocean 125×125 for atmosphere	
Grid spacing	$0.04^{\circ} \times 0.04^{\circ}$	$0.04^{\circ} \times 0.04^{\circ}$ for ocean $0.16^{\circ} \times 0.16^{\circ}$ for atmosphere	
Microphysics scheme Convection scheme PBL scheme Longwave radiation scheme Shortwave radiation scheme Land surface scheme	Not necessary	Various (see Table 3) Various (see Table 3) Various (see Table 3) RRTMG RRTMG Noah land surface model	
Vertical levels	50 (ocean only)	40 (atmosphere) 50 (ocean)	
Initial and boundary conditions	GLORYS (ocean only)	ERA5 (atmosphere) GLORYS (ocean)	
Atmospheric forcings for oceanic model	From ECMWF TIGGE product	From WRF	

Table 1. The computational domain, WRF physics schemes, initial condition, boundary condition, and forcing terms used in the present simulations.

 Table 2.
 MITgcm model physics parameterizations in the present study.

Horizontal Viscosity	Vertical Mixing	Horizontal Diffusion
Simple Harmonic (30 m ² /s) Simple Biharmonic (10 ⁷ m ⁴ /s) SMAGLEITH-Harmonic (30 m ² /s), Smag Coeff 2.5, and Leith Coeff 1.85	K-Profile Parameterization PP81 MY82 GGL90	Implicit Diffusion Explicit Diffusion (100 m ² /s) GMREDI-clipping (100 m ² /s) GMREDI-dm95 (100 m ² /s) GMREDI-ldd92 (100 m ² /s)

Table 3. WRF model physics parameterizations in the present study. The physics options used in the experiments without perturbing the model physics (i.e., CPL.daO and CPL.daS) are highlighted using bold red color.

Microphysics	Convection	Planetary Boundary Layer
Morrison 2-moment	Kain–Fritsch	Mellor–Yamada Nakanishi Niino
Purdue-Lin	Betts-Miller-Janjic	Yonsei University
Thompson	Grell–Freitas Ensemble	Mellor-Yamada-Janjic
WRF single moment 6-class	New Tiedtke	
WRF double moment 6-class	Simplified Arakawa–Schubert	

For validation, we evaluate the daily averaged ocean forecasts and analyses as re-282 sulting from the DA experiments. We first use the assimilated data to examine the time 283 series of innovations and residuals. In addition to the assimilated data, independent ob-284 servations are used. To analyze the subsurface features, we use 206 profiles of temperature and salinity collected between September 15 to October 08 2011 by a joint Woods 286 Hole Oceanography Institute (WHOI) and King Abdullah University of Science and Tech-287 nology (KAUST) cruise along the eastern part of the Red Sea, collected with a horizon-288 tal spacing of 10 km (Zhai et al., 2015). We also use other satellite products to evalu-289 ate the DA results. For SST we select the high-resolution daily averaged level 4 SST prod-290 uct from the Operational Sea Surface Temperature and Sea Ice Analysis (OSTIA, Stark 291 et al., 2007; Donlon et al., 2012) because it is mapped differently with higher resolution. 292 For sea surface height (SSH) we use multimission altimeter merged satellite level 4 grid-293 ded absolute dynamic topography (ADT) provided by CMEMS (hereafter CMEMS-L4, 294 Mertz et al., 2017). Compared with the assimilated CMEMS-L3 data, the CMEMS-L4 295 data is gridded on a 0.25° grid and thus can be used to estimate the errors across the 296 entire Red Sea region. The SSH anomaly from the DA experiments is the instantaneous 297 SSH obtained in the simulations minus the time-averaged SSH from the 15-year MIT-298 gcm model in Sanikommu et al. (2020). The SSH anomalies in CMEMS-L3 and CMEMS-299 L4 are the sea level height above the mean surface based on the long-term averaged ob-300 servations between 1993 to 2012. Because of the lack of in situ observational data of the 301 atmosphere, we use ERA5 to validate the latent heat fluxes and wind speed simulated 302 by the coupled experiments. 303

304 **3 Results**

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The results obtained from the DA experiments are presented in this section. First, 305 we analyze the ensemble spread of the atmospheric forcings and sea surface temperature. 306 Then we examine the ocean states (e.g., SST, SSH, and vertical profiles) to assess the 307 impact of atmospheric forcings in the uncoupled and coupled systems using the valida-308 tion data. In addition to the ocean states, the air-sea exchanges (e.g., latent heat flux) 309 and surface atmospheric states (e.g., wind speed) are also analyzed to illustrate the feed-310 back from the ocean to the atmosphere due to assimilation. Finally, we discuss the changes 311 in the ocean dynamics from assimilating the observation data. 312

3.1 Ensemble Spread Analysis

Similarly to the DA experiments in Sanikommu et al. (2020), we hypothesize that 314 the estimated ocean states are improved when uncertainties in various sources are well 315 accounted for. Incorporating uncertainties in the system improves ensemble spreads in 316 the ocean systematically. For instance, Figs. 2 and 3 display the temporal evolution of 317 atmospheric forcing root-mean-square (RMS) spread in the DA experiments, except for 318 OCN.daO which is forced by the ECMWF ensemble mean. The spread in OCN.daF is 319 from the ECMWF ensemble atmospheric forcing; others are from the coupled model out-320 puts. In comparison with OCN.daF, the spread in CPL.daO is smaller by about one or-321 der of magnitude because the atmospheric models are not perturbed and the spread of 322 atmosphere is from the ocean perturbations. When the SKEB scheme is applied in CPL.daS 323 and CPL.daSP, the spread of the atmospheric forcing is larger than that in OCN.daF, 324 which in turn increases the SST spread, shown in Fig. 4. The impact of the atmospheric 325 forcings on the ocean states will be detailed in the latter sections. 326

327 **3.2 Sea Surface Temperature**

We analyze the SST obtained in our DA experiments to assess its sensitivity to the atmospheric perturbations. The root-mean-square-errors (RMSEs) between the SST analyses and observations in all DA experiments are shown in Fig. 5 and summarized in Ta-



Figure 2. The spatial and temporal evolution of the RMS spread of net surface heat flux Q_{net} along the center line of the Red Sea shown in Fig. 1(c). The Q_{net} is calculated by summing up the latent heat flux, sensible heat flux, net surface shortwave fluxes, and net surface longwave fluxes. Panel (a) shows the spread in the ocean-only experiment driven by ECMWF derived forcing; Panel (b-e) show the spread in the coupled experiments with no perturbations, only SKEB, only perturbed model physics, and SKEB + perturbed model physics, respectively.

ble 4. The best SST forecast and analysis are both from experiment CPL.daSP, when 331 the SKEB scheme is turned on and the WRF physics options are perturbed. The SSTs 332 obtained in the coupled experiments (CPL.daS, CPL.daP, and CPL.daSP; except for the 333 benchmark case CPL.daO) are better than that of the uncoupled experiment OCN.daF, 334 with improvements more than twice larger than standard error of the mean SST from 335 CPL.daSP (about 0.015°C, the standard deviation of SST divided by the square-root 336 of the number of ensemble members). Better improvements are obtained when using only 337 the stochastic forcings (CPL.daS) compared with only perturbing the WRF physics (CPL.daP), 338 but this difference is less significant (smaller than 0.015° C). Although the perturbations 339 in the atmospheric forcing are small in CPL.daO (shown in Figs. 2 and 3), the RMSE 340 errors of SST forecasts and analyses are improved compared to the benchmark exper-341 iment OCN.daO by 0.156°C and 0.101°C, respectively. This indicates that small per-342 turbations of the atmospheric forcing can improve SST in the DA experiments. 343

Figure 5 shows that the RMSEs of SST forecasts and analyses increase in summer for the benchmark runs (i.e., OCN.daO and CPL.daO), but RMSEs get smaller when using the coupled model (i.e., CPL.daS, CPLdaP, and CPL.daSP). In this season, the SST has a larger spread in all the experiments, similar to the results shown in Sanikommu et al. (2020), likely because the ocean is more sensitive to heat fluxes when the mixed layer depth is shallower.

In addition to the assimilated data, we validated the SSTs using the OSTIA SST. The RMSEs and correlations are shown in Fig. 6 and summarized in Table. 4. We present the SST correlations to evaluate the forecast of the SST evolution during the year. It can be seen that the SST obtained in CPL.daSP has larger correlations and smaller RM-



Figure 3. The spatial and temporal evolution of the RMS spread of 10-m wind speed along the center line of the Red Sea shown in Fig. 1(c). Panel (a) shows the spread from the ECMWF derived forcing; Panel (b-e) show the spread in the coupled experiments with no perturbations, only SKEB, only perturbed model physics, and SKEB + perturbed model physics, respectively.

SEs in the north Red Sea, center Red Sea, and Gulf of Aden regions. Compared with 354 the uncoupled experiment OCN.daF, the coupled experiment CPL.daSP has a smaller 355 RMSE by 0.035° C (6.5%, more than twice the standard error). On the other hand, the 356 SST analysis obtained in CPL.daSP has a slightly larger RMSE compared to that ob-357 tained in CPL.daF, but the differences between OCN.daF, CPL.daS, CPL.daP, and CPL.daSP 358 are within $0.01^{\circ}C$ (2%). In addition, the CPL.daSP also has the smallest distance be-359 tween the forecasts and analyses RMSEs, indicating less "assimilation shock" and more 360 balanced ocean states in the DA experiment. 361

362 **3.3 Sea Surface Height**

The SSH fields as estimated in the DA experiments are presented in Fig. 7 and Ta-363 ble 5. Similar to the SST results, the coupled DA experiments exhibit smaller RMSE 364 and larger spread. The SSH forecast errors in OCN.daF, CPL.daS, CPL.daP, and CPL.daSP 365 are not significantly different. Although CPL.daSP still has the smallest RMSEs, the dif-366 ferences are within 1% and smaller than the standard errors (about 0.001 m). For the 367 SSH analyses, on the other hand, the CPL.daS and CPL.daSP are more significantly im-368 proved (RMSEs are smaller by 10% compared with OCN.daF and CPL.daP) when SKEBS are used, suggesting that including the stochastic forcing in model parameters is the key 370 for improvements. Note that the spread of surface wind forcing shown in Fig. 3 is greatly 371 increased when using the stochastic forcing. 372

The temporal evolution of the SSH is also examined by comparing with CMEMS-L4 data, shown in Fig. 8. Here we only highlight the differences of the SSH analyses because the forecasts are close to each other. Figure. 8 shows that the CPL.daSP experiment has larger correlations and smaller RMSEs in both the Red Sea and the Gulf of Aden regions. Similar to the results shown in Fig. 7, when using the stochastic forcings



Figure 4. The spatial and temporal evolution of the RMS spread of Sea Surface Temperature along the center line of the Red Sea shown in Fig. 1(c). Panel (a) shows the spread in the oceanonly experiment driven by ECMWF derived forcing; Panel (b-e) show the spread in the coupled experiments with no perturbations, only SKEB, only perturbed model physics, and SKEB + perturbed model physics, respectively.

Table 4. SST obtained in the DA experiments against the validation data. We highlighted the best forecast/analysis using red, but the pink color is used when the differences between uncoupled and coupled experiments are insignificant (when the RMSE difference is smaller than 5% or the standard error).

	OCN.daO	OCN.daF	CPL.daO	CPL.daS	CPL.daP	CPL.daSP
Against assimilated data						
SST forecast RMSE	0.656	0.486	0.500	0.419	0.426	0.403
SST analysis RMSE	0.475	0.341	0.374	0.281	0.294	0.262
Against OSTIA SST						
SST forecast RMSE	0.650	0.574	0.610	0.560	0.551	0.539
SST analysis RMSE	0.486	0.463	0.484	0.468	0.472	0.469
SST forecast correlation	0.9580	0.9623	0.9573	0.9637	0.9628	0.9649
SST analysis correlation	0.9786	0.9805	0.9773	0.9800	0.9788	0.9791
SST forecast spread	0.078	0.080	0.077	0.098	0.095	0.108
SST analysis spread	0.046	0.052	0.048	0.059	0.055	0.062

in WRF, CPL.daS and CPL.daSP outperform the uncoupled model OCN.daF (see Ta-378 ble 5).

379



Figure 5. Time history of SST RMSEs and spreads during the data assimilation experiment. Panels (a) and (c) show the RMSEs of the forecasts and analyses against the assimilated data; Panels (b) and (d) show the spread of SST in the forecasts and analyses. The yellow dots in Panels (a) and (c) indicate the total uncertainty (square root of the sum of ensemble variance and observational variance $(0.5^{\circ}C)^{2}$) of CPL.daSP.

3.4 Temperature and Salinity Profiles

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The subsurface features of the ocean are validated against independent (i.e. not 381 assimilated) CTD observations of temperature and salinity from the WHOI/KAUST sum-382 mer cruise in the Red Sea between September 15 and October 08 2011. The difference 383 between daily averaged forecasts and observations is shown in Figs. 9 and 10. More than 384 2 degree and 0.8 psu differences are found for temperature and salinity profiles in the 385 thermocline between 50–100 m. For the temperature profiles, the RMSE in CPL.daSP $(0.361^{\circ}C)$ 386 is smaller than OCN.daO $(0.408^{\circ}C)$ by about 10%, especially near the ocean surface, but 387 within 2% difference compared to OCN.daF, CPL.daO, and CPL.daS. For the salinity 388 profiles, the forecast RMSE of CPL.daSP (0.082 psu) is smaller than the benchmark ex-389 periment OCN.daO by about 30%. It is noted that CPL.daP has the smallest RMSE 390 for temperature $(0.344^{\circ}C)$, but its salinity RMSE is significantly larger (0.122 psu) than 391 CPL.daSP. Compared with the ocean-only experiment OCN.daF, the RMSEs in CPL.daS 392 and CPL.daSP are not significantly different (within 1% or 2%). Although the coupled 393 experiment is no better than the best uncoupled experiment OCN.daF, the results in-394 dicate the stochastic schemes in WRF are crucial for producing better forecasts of the 395 ocean profiles. 396



Figure 6. SST RMSEs and correlations obtained in the DA experiments validated against OSTIA. Panels (a) and (b) show the RMSE and correlation of the "forecast" SST. The contours in column 1 indicate the comparison with OSTIA data; columns 2-5 are normalized by the reference OCN.daO in column 1 to highlight differences, showing the ratios in percentage.

Table 5. Summary of SSH against the validation data. We highlighted the best forecast/analysis using red, but the pink color is used when the differences between coupled and coupled experiments are insignificant (when the RMSE difference is smaller than 5% or the standard error).

	OCN.daO	OCN.daF	CPL.daO	CPL.daS	CPL.daP	CPL.daSP
Against assimilated data						
SSH forecast RMSE	0.0646	0.0626	0.0650	0.0624	0.0626	0.0620
SSH analysis RMSE	0.0580	0.0495	0.0578	0.0446	0.0522	0.0433
Against CMEMS-L4 SSH						
SSH forecast RMSE	0.0513	0.0486	0.0513	0.0483	0.0494	0.0482
SSH analysis RMSE	0.0461	0.0390	0.0455	0.0356	0.0409	0.0350
SSH forecast correlation	0.9121	0.9197	0.9109	0.9197	0.9168	0.9204
SSH analysis correlation	0.9314	0.9493	0.0320	0.9578	0.9439	0.9590
SSH forecast spread	0.0034	0.0056	0.0036	0.0073	0.0048	0.0076
SSH analysis spread	0.0023	0.0038	0.0024	0.0046	0.0032	0.0047

3.5 Feedback to the Atmosphere

397

To assess the impact of ocean data assimilation on the surface of the atmosphere, we compare the latent heat fluxes and 10-m wind speed obtained in the DA experiments. This analysis informs feedback to the heat and momentum fluxes. We consider ERA5 as reference and present the RMSEs of latent heat fluxes and 10-m wind speed in Fig. 11. Here we only compare the data on the centerline of the Red Sea to highlight ocean regions. It can be seen that the RMSEs do not grow significantly with time, showing the capability of the coupled system for the 1-year DA experiments. We hypothesize this is



Figure 7. Evolution of the SSH RMSEs and spreads during the data assimilation experiment. Panels (a-b) show the RMSEs of the forecasts and analyses against the assimilated data; Panels (c-d) show the RMS spread of SSH in the forecasts and analyses. The yellow dots in Panels (a) and (c) indicate the total uncertainty (square root of the sum of ensemble variance and observational variance $(0.04 \text{ m})^2$) of CPL.daSP.

because the atmospheric states are constrained by the boundary conditions for this rel-405 atively small domain. Compared with the RMSEs of latent heat flux and 10-m wind speed 406 in the benchmark case CPL.daO (62.9 W/m^2 and 1.52 m/s), the CPL.daSP (60.2 W/m^2 407 and 1.47 m/s) has smaller errors by about 4%, but the RMSE differences are smaller than 408 the standard error $(3.1 \text{ W/m}^2 \text{ and } 0.09 \text{ m/s})$, implying the improved ocean states may 409 not significantly impact the atmospheric states. Because of the small differences in the 410 surface atmosphere, this indicates that for the Red Sea region, the skill of the coupled 411 model is not from the two-way coupling, but from the atmospheric forcings in the down-412 scaled WRF ensembles (one-way coupled) to drive the ocean model. 413

3.6 Vertical Current Velocity

414

Toye et al. (2017) argued that the dynamical balances (or assimilation shock) in 415 the oceanic model from the EAKF increments increase the spread of the Red Sea fore-416 casts. The imbalances are also reported in other EAKF assimilation experiments (L. A. An-417 derson et al., 2000; Hoteit et al., 2010; Park et al., 2018). Here, we investigate the dy-418 namical balances in our experiments by comparing the standard deviation of |w| obtained 419 in the DA experiments with the "free" run without assimilating observation data in Fig. 12. 420 The results show that the spreads of |w| in all DA experiments are larger than the "free" 421 run for the Red Sea region, but the changes in |w| spread in CPL.daSP are close to the 422



Figure 8. SSH RMSEs and correlations obtained in the DA experiments validated against CMEMS-L4 data. Panels (a) and (b) show the RMSEs and correlations of the SSH analyses. The contours in column 1 indicate the comparison with CMEMS-L4 data; columns 2-5 are normalized by the reference OCN.daO in column 1 to highlight differences, showing the ratios in percentage

ocean-only model experiment OCN.daF, indicating no significant dynamical imbalances
 are introduced when using the coupled model.

425 4 Summary and Conclusions

This work implemented a data assimilation framework based on the regional coupled model SKRIPS and DART. Using the EAKF in DART, we investigate the impact of ocean data assimilation on the oceanic and atmospheric states of the Red Sea. The coupled system assimilates satellite-based sea surface temperature and height and in situ temperature and salinity glider profiles every 3 days for 1 year starting from January 01, 2011.

To assess the performance of the ensemble forecasts and examine the generated ocean 432 states, we ran a series of experiments using different perturbation schemes. The assim-433 ilation results of the coupled experiments are compared with the uncoupled ones forced 434 by ECMWF-derived surface forcing, revealing that the coupled experiments give greater 435 spread in the ensembles of ocean states, with the spread continuing to increase when us-436 ing the stochastic kinetic energy backscatter (SKEB) scheme. Compared with the as-437 similated data, the coupled experiments result in a more skillful SST and SSH ensem-438 ble mean forecast. The SST forecasts and SSH analyses in coupled models are also bet-439 ter than uncoupled ones when compared with the independent observational data, but 440 the RMSEs of SST analyses and SSH forecasts are insignificantly different. 441

We further compared the DA experiment results with the independent cruise ob-442 servation data of temperature and temperature profiles. The comparison shows large vari-443 ations in the temperature profiles because of the challenge in modeling the thermocline 444 layer and the lack of in situ data. The RMSEs from the coupled DA experiments with 445 perturbations of the atmospheric model are comparable to the uncoupled model driven 446 by ECMWF-derived ensemble forcing, and both are better than the benchmark exper-447 iments with small spreads in atmospheric forcings. To investigate the feedback from the 448 ocean, we validated the latent heat flux and 10 m winds in all coupled experiments us-449 ing ERA5 data, but no significant difference is observed. 450



Figure 9. The differences between the temperature at 0-300 m obtained in the DA experiments compared to in situ observations (results minus observations).

This study demonstrates that our Red Sea DA system using two-way coupled model with WRF performs better or equal to an uncoupled model driven by ECMWF-derived ensemble surface forcing, showing a promising approach for forecasting the oceanic states or producing ocean analysis data. The dynamical imbalances in the coupled model are also not significantly different from the uncoupled model. The DA system implemented here explores the utility of a coupled DA system and studies of the ocean–atmosphere interactions using the analysis data.

458 Acknowledgments

We gratefully acknowledge the research funding (grant number: OSR-2022-NCM-4829.5) 459 from KAUST (King Abdullah University of Science and Technology). We also appre-460 ciate the computational resources of the supercomputer Shaheen II and the assistance 461 provided by KAUST Supercomputer Laboratory. RS and ACS were supported by ONR 462 ASTRAL research initiative (N00014-23-1-2092). ACS was supported by NOAA Grant 463 NA18OAR4310405 and ONR MISOBOB research initiative (N00014-17-S-B001). BDC 464 and MRM were supported by NOAA Grant NA21OAR4310257, NA18OAR4310403, and 465 NA22OAR4310597. AJM was partly supported by the National Science Foundation (OCE-466 2022868). We appreciate Luca Delle Monache, Daniel Steinhoff, and Rachel Weihs for 467 discussing the generation of WRF ensembles. 468

469 Data Availability Statement

The coupled model used for the simulations is available at https://github.com/ iurnus/scripps_kaust_model. The DA experimental results used in the paper are available at https://zenodo.org/records/10408667.



Figure 10. The differences between the salinity at 0-300 m obtained in the DA experiments in comparison with in situ observations (results minus observations).

473 Author contributions statement

All authors conceived the experiments; R.S. implemented the DA system for the
coupled models; S.S. implemented the DA system for the uncoupled models and the ROCOTO workflow; R.S. conducted the experiments and plotted the figures; R.S. and S.S.
drafted the initial manuscript; all authors discussed the results and revised the manuscript.

478 Competing Interests

480 References

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The authors declare no competing interests.



Figure 11. The RMSEs of latent heat flux and 10-m wind speed obtained in the coupled model when assimilating the ocean data. We only compare the data on the centerline of the Red Sea.

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